



**Forschungsseminar Algebra und Zahlentheorie**  
**Prof. E. Große-Klönne / Prof. T. Schmidt**

Wintersemester 2013/14

**Vorträge im Dezember 2013/Januar 2014**

Minikurs von **Prof. Kazim Buyukboduk, Koc Univ. Istanbul**

**Titel: Beilinson-Kato elements and the  $p$ -adic BSD conjecture of Mazur-Tate-Teitelbaum**

**Abstract:** In order to formulate a  $p$ -adic Birch and Swinnerton conjecture(BSD for short) for an elliptic curve  $E$ , Mazur, Tate and Teitelbaum (MTT) constructed a  $p$ -adic  $L$ -function attached to  $E$ . To understand its compatibility with the usual BSD, one needs to compare the order of vanishing of the  $p$ -adic  $L$ -function at  $s=1$  to that of the Hasse-Weil  $L$ -function (where the latter is called the analytic rank of  $E$ ). When  $E$  has split multiplicative reduction mod  $p$ , MTT observed that the  $p$ -adic  $L$ -function always vanishes at  $s=1$  and they conjectured that its order of zero is exactly one more than the analytic rank of  $E$ . In 1992, Greenberg and Stevens proved this conjecture when the analytic rank is zero.

In the first two lectures of this talk, I will explain a proof of the MTT conjecture when the analytic rank is one. The main ingredients for the proof are the Beilinson-Kato elements in the  $K_2$  of modular curves and a Gross-Zagier-style formula we prove for the  $p$ -adic height of the Beilinson-Kato elements. In the last part of the talk, I will discuss an extension (in a joint work with D. Benois) of this result to the case of a modular form  $f$  of weight greater than 2. The main difficulty in this case lies in the fact the Galois representation  $V$  attached to  $f$  by Deligne, in the presence of "extra zeros", is no longer  $p$ -ordinary. This difficulty is circumvented relying on the fact that the (local Galois representation)  $V$  admits a triangulation over the Robba ring (thence it is **\*ordinary\*** in the level of the associated  $\varphi_{\Gamma}$ -modules).

**11.12.2013**

**Lecture 1**

Basics: Elliptic curves, BSD,  $p$ -adic BSD and Iwasawa theory, Kato's Euler system and applications.

**18.12.2013**

**Lecture 2**

Nekovar's Selmer complexes and  $p$ -adic heights, a (higher)  $p$ -adic Gross-Zagier formula and the conjecture of Mazur-Tate-Teitelbaum.

**22.01.2014**

**Lecture 3**

Galois representations attached to modular forms, triangulations and the MTT conjecture for modular forms of higher weight (joint work with Denis Benois).

Prof. E. Große-Klönne

Prof. T. Schmidt

Alle Interessenten sind herzlich eingeladen.

**Die Vorträge finden Rudower Chaussee 25, 12489 Berlin, Raum 2.009, statt. Zeit: 11-13 Uhr.**

Verkehrsverbindungen

S-Bahn  
Bus  
Tram

S-Bahnhof Adlershof  
Linie 162, 164 (Richtung Schönefeld/Rudow) – 2 Stationen bis Magnusstr.  
Linie 60, 61 (Richtung Karl-Zieger-Str.)

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