## EXERCISE SHEET 1

## GRAPH COMPLEXES, SUMMER 23, HU BERLIN

Exercise 1. Show that the two graphs below are isomorphic.


Are the following two graphs isomorphic?


Exercise 2. Endow the graph $G=\square$ with an orientation and compute its differential.

Exercise 3. Consider the cycle graph on $n$ vertices $C_{n}$ and the wheel with $n$ spokes $W_{n}$,


For which $n \in \mathbb{N}$ do they represent
(1) non-zero elements in $G C_{0}$ ?
(2) cycles in $G C_{0}$ ?
(3) non-trivial classes in $H\left(G C_{0}\right)$ ?
(in the case $C_{n}$ we work in the larger complex $G C_{0}^{v \geq 2}$ where vertices of valence 2 are allowed)

