

**EXERCISE III**  
**(MAY 22 2013, TO BE HANDED IN JUNE 05 2013)**

DYSON SCHWINGER EQUATIONS (KREIMER, SUMMER '13)

- 1.  
Let  $v_i$  be the sum of all 1PI graphs for the photon self-energy in QED. Let  $I$  be the co-ideal for the Ward Identity of QED, its  $k$ -loop components  $i_k$  are the sum of all 1PI  $k$ -loop graphs for the QED vertex plus fermion self-energy.  
Show:  $\Delta'(v_3) = 2i_2 \otimes v_1 + 4i_1 \otimes v_2 + v_1 \otimes v_2$ .
- 2.  
Try to give a formula for  $\Delta'(v_k)$ .
- 3.  
Consider a QED-like theory with two different photons initiated by decoupled gauge groups  $U(1) \times U(1)$ . What is the co-ideal structure which you expect?