## EXERCISE IV (JUNE 05 2013, TO BE HANDED IN JUNE 19 2013)

DYSON SCHWINGER EQUATIONS (KREIMER, SUMMER '13)

## • 1.

Consider a theory with one type of unoriented edge, and vertices of valence  $2 < k \leq k_0$ , of order  $g^{k-2}$ . Write down the combinatorial Dyson–Schwinger equations for the  $2 \leq m$ -point functions restricting to one-loop Hochschild one-cocycles. Determine  $B^{1;m}_+$  in terms of graphs  $B^{\gamma}_+$ .

• 2.

What is the co-ideal structure? What happens for  $k_0 \to \infty$ ?

• 3.

Read D. Kreimer and A. Velenich, *Field diffeomorphisms and the algebraic structure of perturbative expansions*, Lett. Math. Phys. **103** (2013) 171, [arXiv:1204.3790 [hep-th]]. Relate the paper to the above exercises.