QFT II (Kreimer, Summer 2014)

Exercise III (May 28 2014, to be handed in June 11 2014)

1.(10 points)

In ϕ_4^4 theory, determine all graphs contributing to the self-energy up to two loops and determine their symmetry factors.

2.(10 points)

Determine their renormalized integrands in parametric renormalization. Use renormalization conditions such that the self-energy $\Sigma(q^2, m^2)$ vanishes at $q^2 = m^2$, and its derivative wrt q^2 as well: $\Sigma'(q^2, m^2)_{q^2=m^2} = 0.$

3.(10 points)

Introduce Z-factors into each monomial in the Lagrangian. Determine them to one-loop order for the two monomials quadratic in the fields using either dimensional regularization or a cut-off c in parametric renormalization so as to fulfill the above renormalization conditions.