Lorentzian Spin Manifolds with "many" Parallel Spinors

Lana Casselmann

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Abstract

During last semester's talk, we introduced the notion of a Killing spinor and defined $\kappa(M, \lambda) := \frac{\dim S(\lambda)}{\operatorname{rankS}}$, where S is the spinor bundle over a semi-Riemannian spin manifold and $S(\lambda)$ is the vector space of Killing spinors with Killing number λ . We then considered some cases of a given lower boundary for $\kappa(M, \lambda)$ and the consequences thereof.

During this talk, we will consider the special case of a Lorentzian spin manifold with $\kappa(M,0) =: \kappa(M) > \frac{1}{2}$. Using some aspects of holonomy theory, we will show that such a manifold has to be flat.